Wouter van Limbeek

Research interests:

My research focuses on group actions on manifolds and other geometric objects. These occur everywhere in geometry and topology, and their study offers a rich interplay between differential geometry, geometric topology, geometric group theory and Lie theory. A very general problem in this context is to relate the geometry of a manifold M and the algebraic structure of groups acting on M. For instance, if M is a given manifold, which groups G can act on Misometrically (with respect to some Riemannian metric)? Preserving a volume form? Such that a lattice acts properly discontinuously and cocompactly?

Inspired by work of Farb and Weinberger, I recently proved that if M is a closed Riemannian manifold such that the isometry group of the universal cover $\text{Isom}(\widetilde{M})$ is connected and noncompact, then a finite cover of M is a fiber bundle over a locally homogeneous space associated to $\text{Isom}(\widetilde{M})$. Equivalently, if a connected Lie group acts properly on a simply connected manifold X such that a lattice Γ acts freely and cocompactly, then a finite cover of X/Γ is a fiber bundle over a locally homogeneous space.

Currently I am investigating possible generalizations of this result to situations where G does not preserve a Riemannian metric, but a different geometric structure (e.g. a pseudo-Riemannian metric or a conformal structure).