

**GLOBAL EXISTENCE FOR
VOLTERRA–FREDHOLM TYPE NEUTRAL
IMPULSIVE FUNCTIONAL
INTEGRODIFFERENTIAL EQUATIONS**

V. Vijayakumar, S. Sivasankaran and M. Mallika Arjunan

Abstract. In this paper, we study the global existence of solutions for the initial value problems for Volterra-Fredholm type neutral impulsive functional integrodifferential equations. Using the Leray-Schauder's Alternative theorem, we derive conditions under which a solution exists globally. An application is provided to illustrate the theory.

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V. Vijayakumar
 Department of Mathematics,
 Info Institute of Engineering,
 Kovilpalayam, Coimbatore-641 107,
 Tamilnadu, India.
 e-mail: vijaysarovel@gmail.com

S. Sivasankaran
 Department of Mathematics,
 University College,
 Sungkyunkwan University,
 Suwon 440-746, South Korea.
 e-mail: sdsiva@gmail.com.

M. Mallika Arjunan
 Department of Mathematics,
 Karunya University,
 Karunya Nagar, Coimbatore-641 114,
 Tamilnadu, India.
 e-mail: arjunphd07@yahoo.co.in
